

# 1 When does female multiple mating evolve to adjust 2 inbreeding? Effects of inbreeding depression, direct 3 costs, mating constraints, and polyandry as a 4 threshold trait

5 Supporting Information S2: Distributions of allele and trait values, inbreeding coefficients,  
6 neutral alleles, inbreeding adjustment, and trait correlations for conditional polyandry.

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11 Here we present supplemental results from an individual-based model in which  
12 alleles underlying inbreeding strategy ( $I_a$ ) and polyandry ( $P_a$ ) affect phenotypic  
13 values for inbreeding strategy and polyandry ( $I_p$  and  $P_p$ , respectively) given dif-  
14 ferent magnitudes of inbreeding depression ( $\beta$ ), direct costs of the polyandry  
15 phenotype ( $c_P$ ), and constraints on initial versus additional mate availability  
16 ( $S_{initial,additional}$ ) when polyandry is conditional upon females having access to  
17 a higher quality additional male than their initial male. Specifically, we present  
18 distributions of allele and phenotype values not shown in the main text, distri-  
19 butions of inbreeding coefficients, distribution of neutral allele values ( $\eta$ ), dis-  
20 tributions of inbreeding adjustment ( $k_{adj}$ ), and distributions of mean among in-  
21 dividual correlations between  $I_g$  and  $P_g$ . Overall, polyandry was adaptive over a  
22 much wider range of parameter values than when polyandry was not conditiona,  
23 but the magnitude of inbreeding adjustment remained consistently small.

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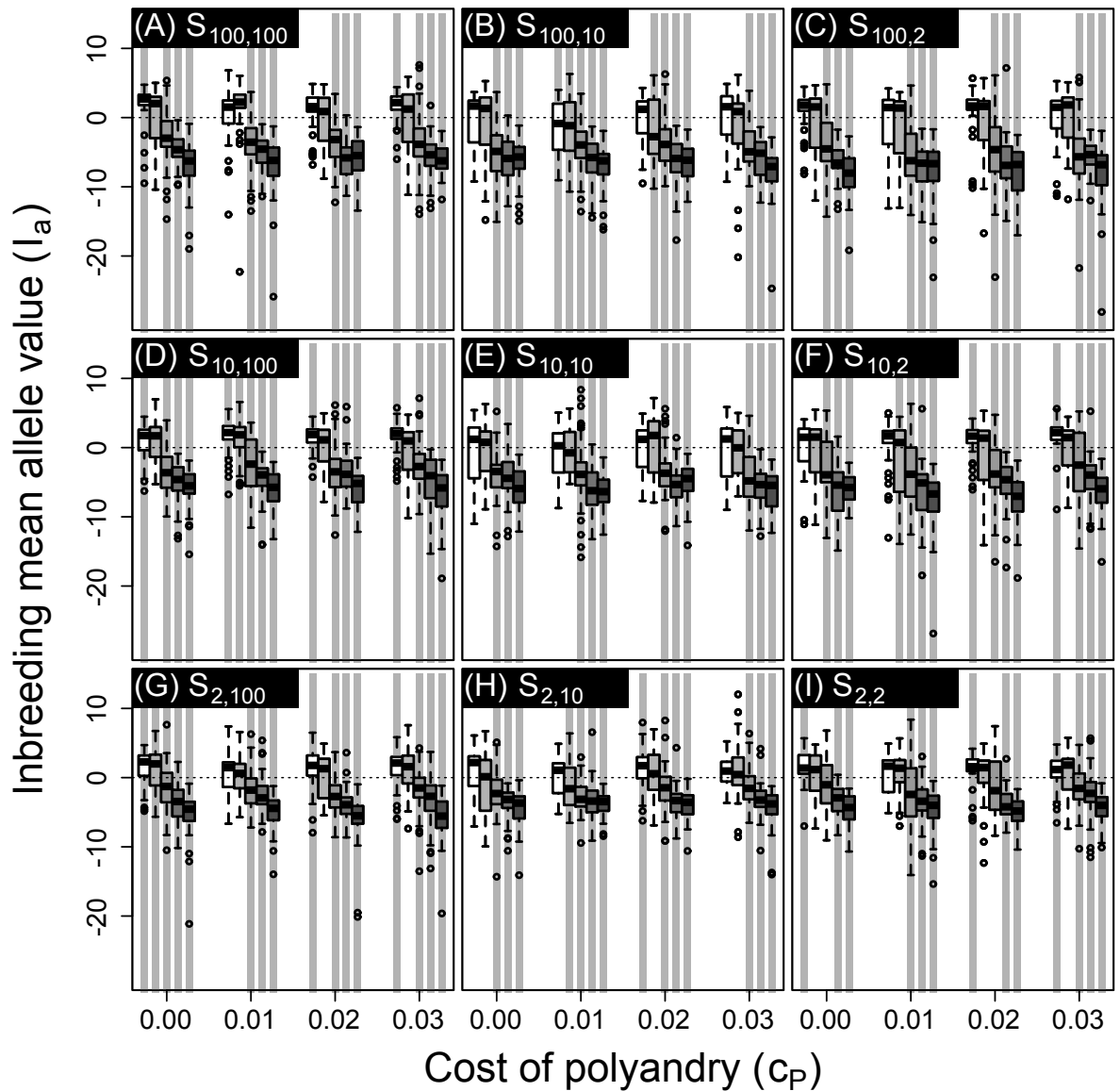
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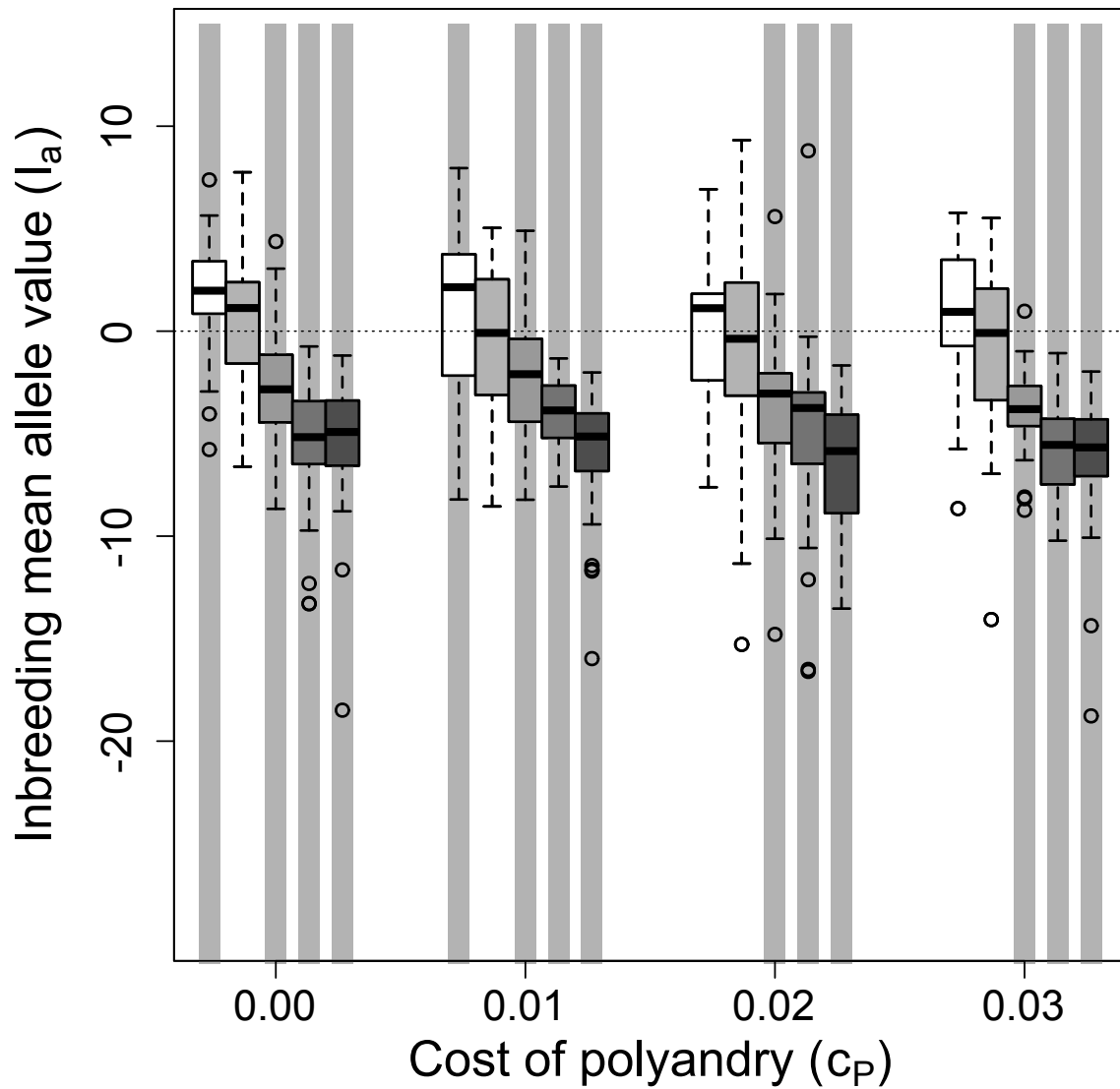
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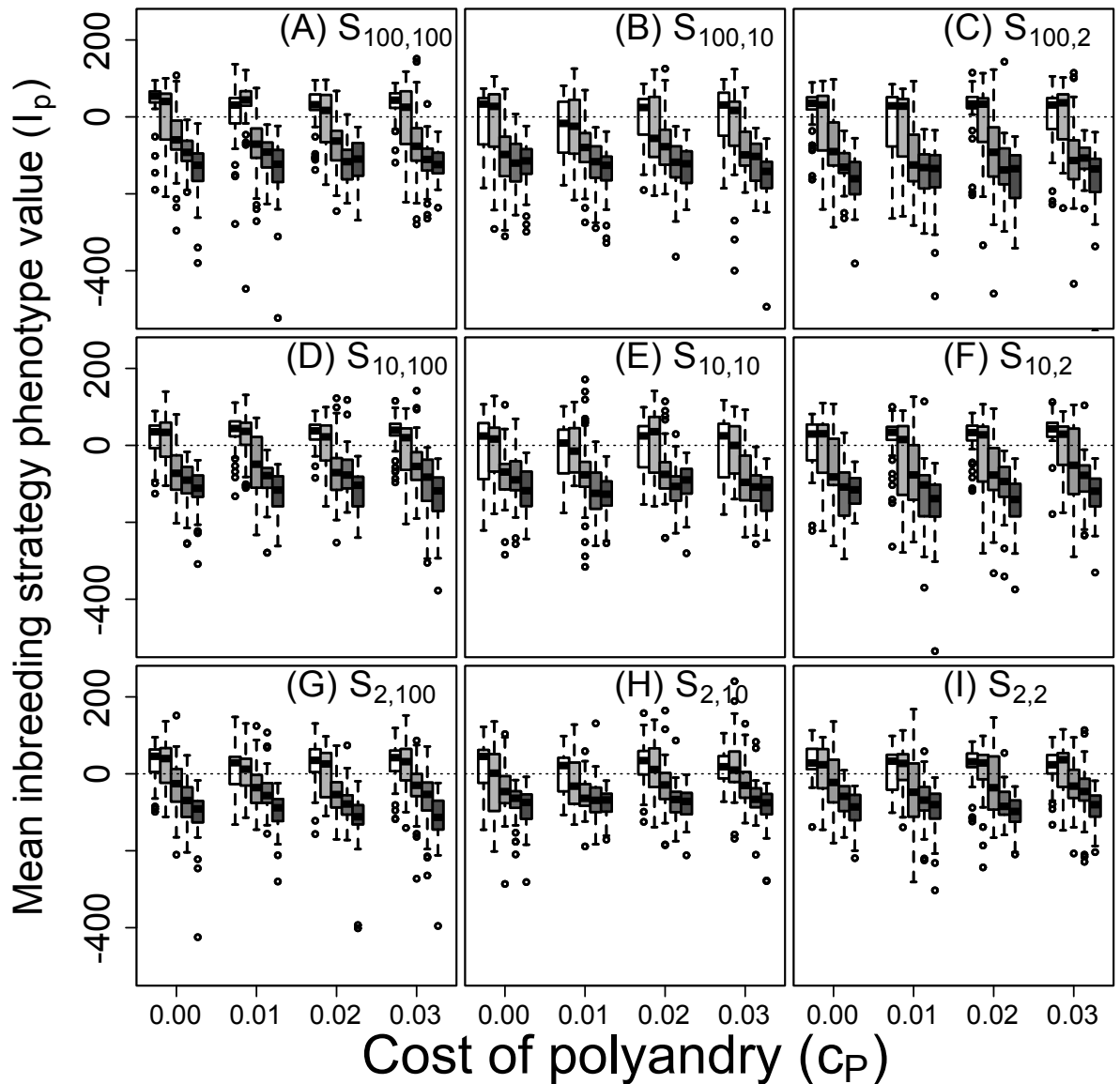
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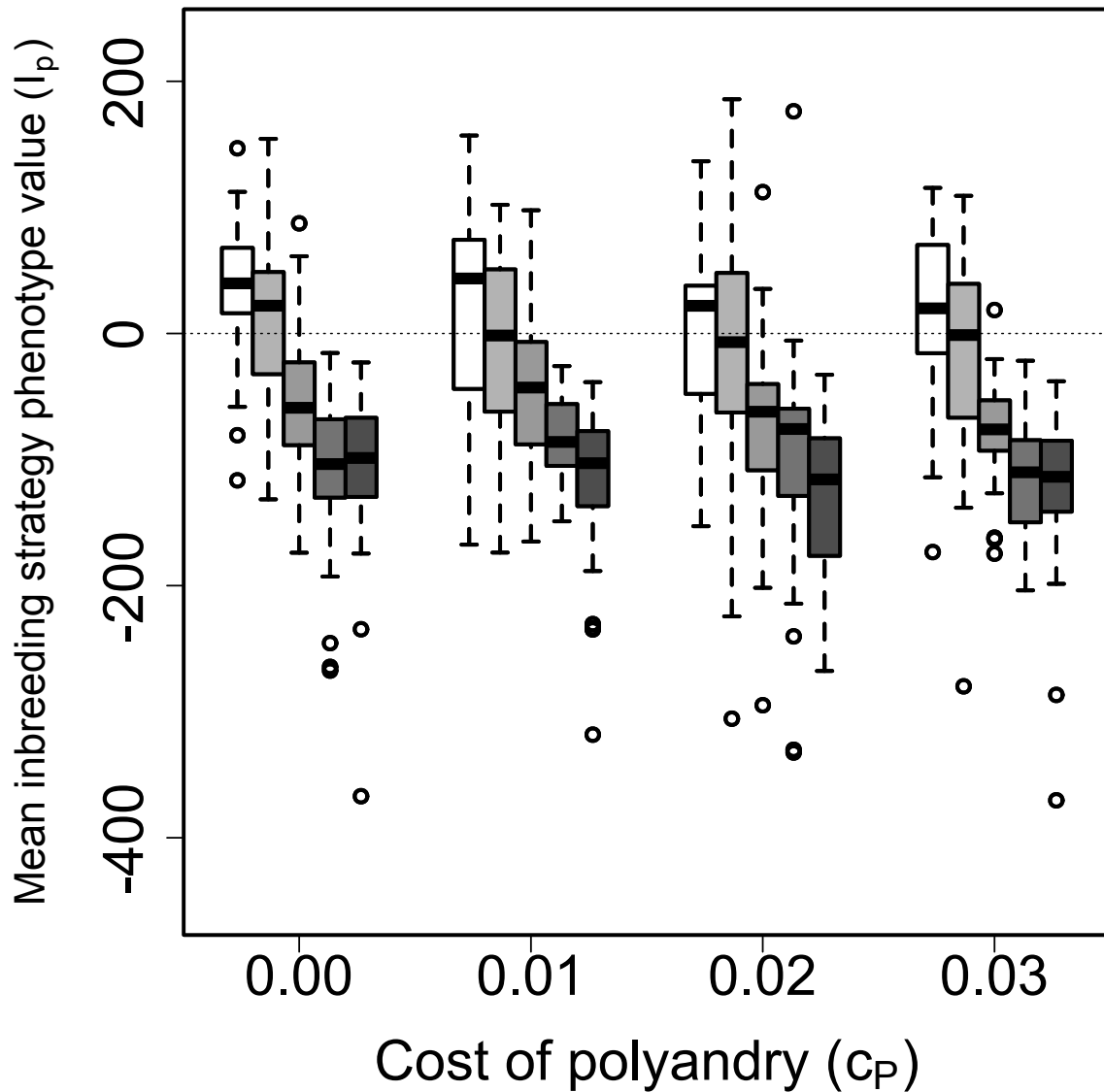
**Figure S2-1:** Distributions of mean inbreeding allele value ( $I_a$ ) after 5000 simulated generations across replicates with different parameter combinations. Panels show different combinations of initial versus additional male availability ( $S_{initial,additional}$ ) for choosing females. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five increasingly severe magnitudes of inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis. Grey vertical bars highlight replicate simulations in which expected values (i.e., grand means) of mean  $I_a$  are positive and 95% bootstrapped confidence intervals do not overlap zero.



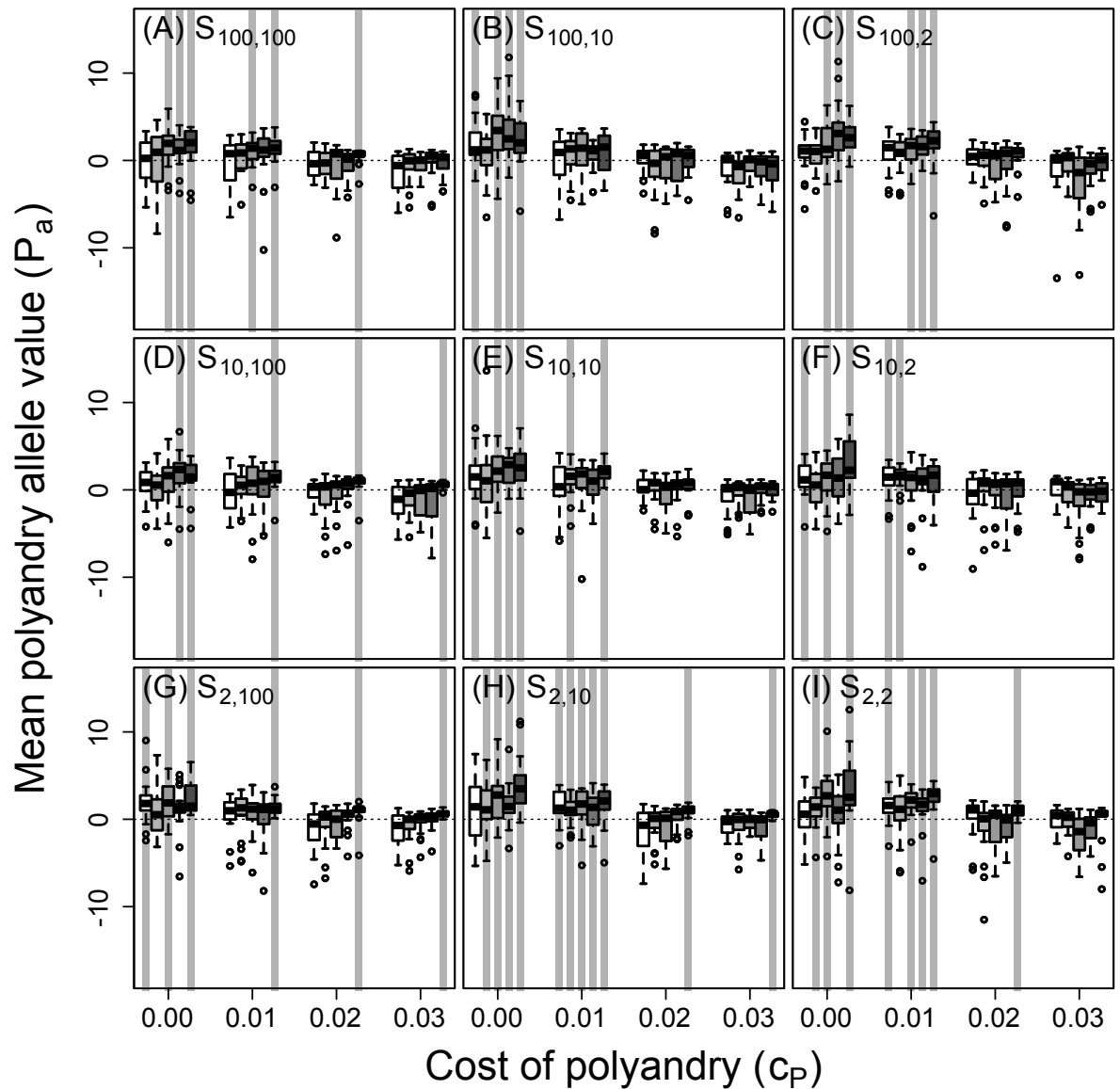
**Figure S2-2:** Distributions of mean inbreeding allele value ( $I_a$ ) after 5000 simulated generations across replicates with different parameter combinations. Male availability is socially constrained ( $S_{Q,100}$ ) such that females choosing their initial mates only have access to males not already chosen by other females. Blocks of boxes show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. The dotted horizontal line indicates zero on the y-axis. Grey vertical bars highlight replicate simulations in which expected values (i.e., grand means) of mean  $I_a$  are positive and 95% bootstrapped confidence intervals do not overlap zero.



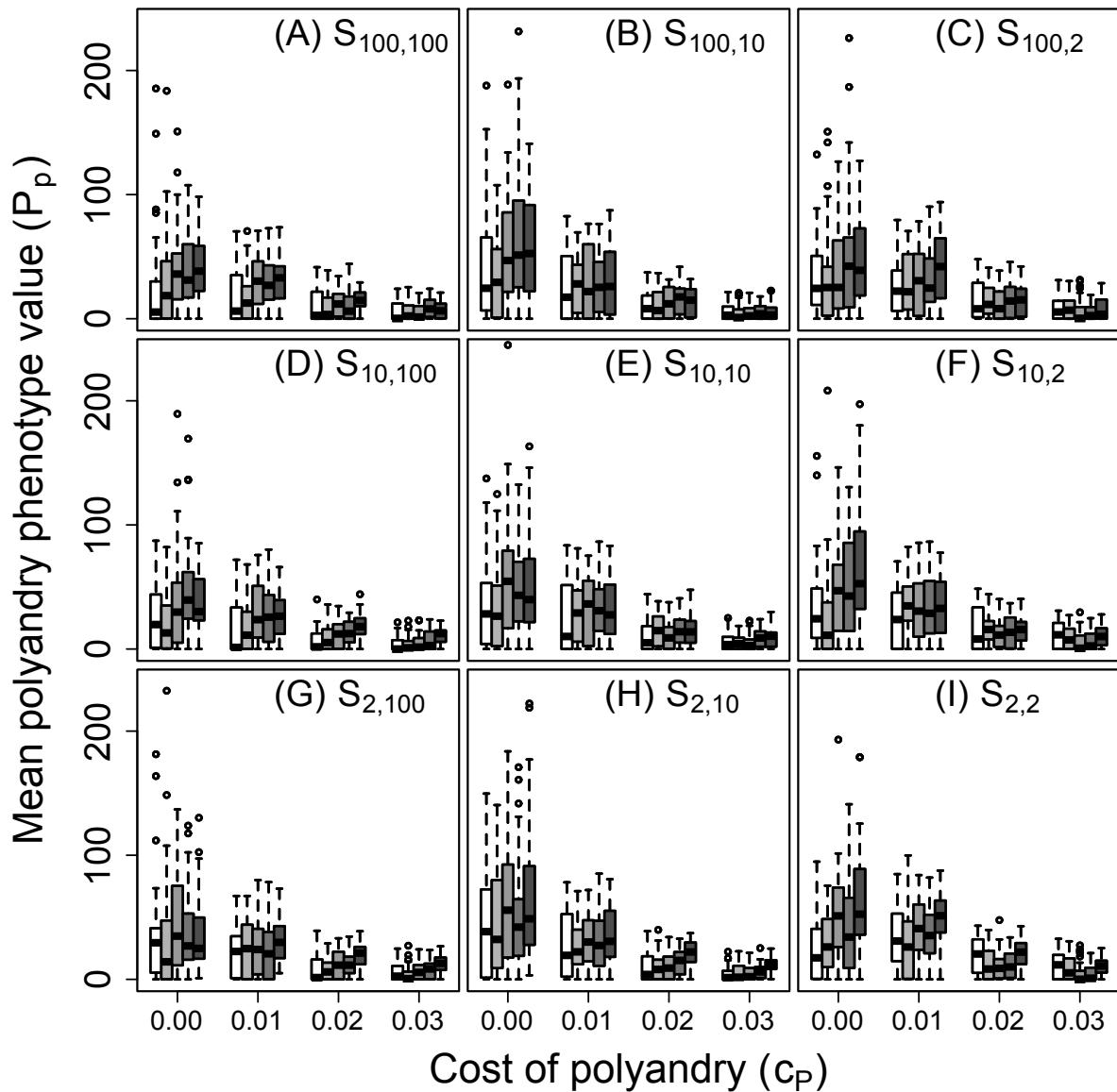
**Figure S2-3:** Distributions of mean inbreeding strategy phenotype value ( $I_p$ ) after 5000 simulated generations across replicates with different parameter combinations. Panels show different combinations of initial versus additional male availability ( $S_{initial,additional}$ ) for choosing females. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis.



**Figure S2-4:** Distributions of mean inbreeding strategy phenotype value ( $I_p$ ) after 5000 simulated generations across replicates with different parameter combinations. Male availability is socially constrained ( $S_{Q,100}$ ) such that females choosing their initial mates only have access to males not already chosen by other females. Blocks of boxes show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. The dotted horizontal line indicates zero on the y-axis.

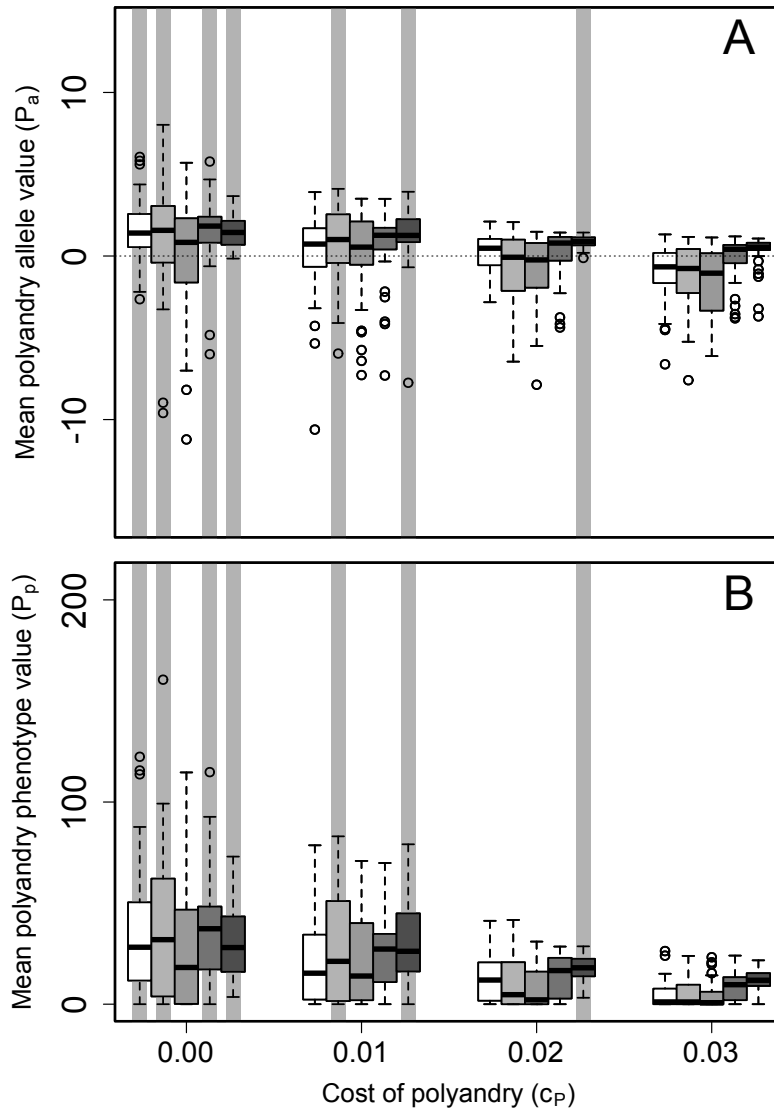


**Figure S2-5:** Distributions of mean polyandry allele value ( $P_a$ ) after 5000 simulated generations across replicates with different parameter combinations where polyandry is conditional. Panels show different combinations of initial versus additional male availability ( $S_{initial,additional}$ ) for choosing females. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five increasingly severe magnitudes of inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis. Grey vertical bars highlight replicate simulations in which expected values (i.e., grand means) of mean  $P_a$  are positive and 95% bootstrapped confidence intervals do not overlap zero.

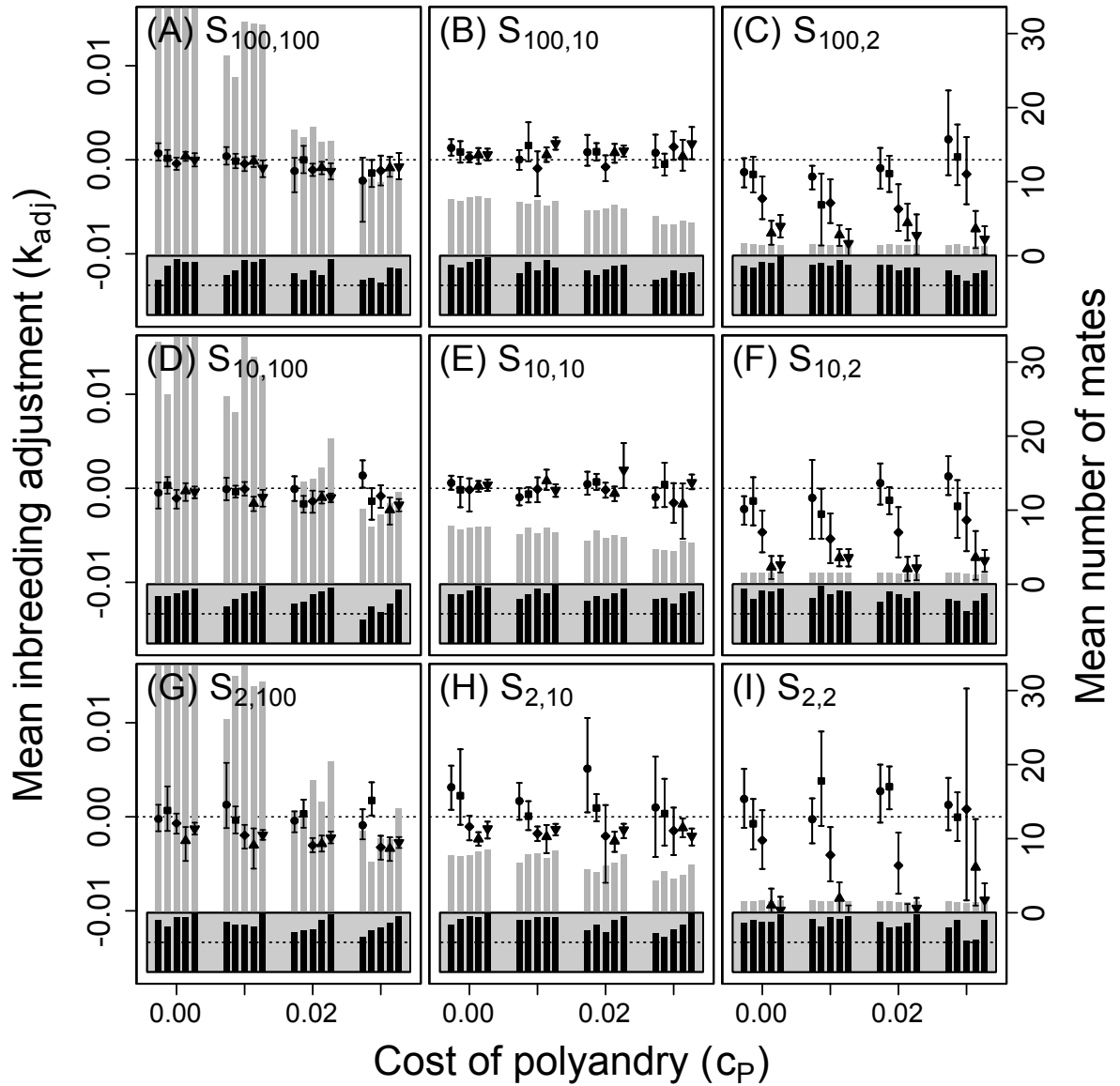


**Figure S2-6:** Distributions of mean polyandry phenotype value ( $P_p$ ) after 5000 simulated generations across replicates with different parameter combinations when polyandry is conditional. Panels show different combinations of initial versus additional male availability ( $S_{initial,additional}$ ) for choosing females. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five increasingly severe magnitudes of inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis.

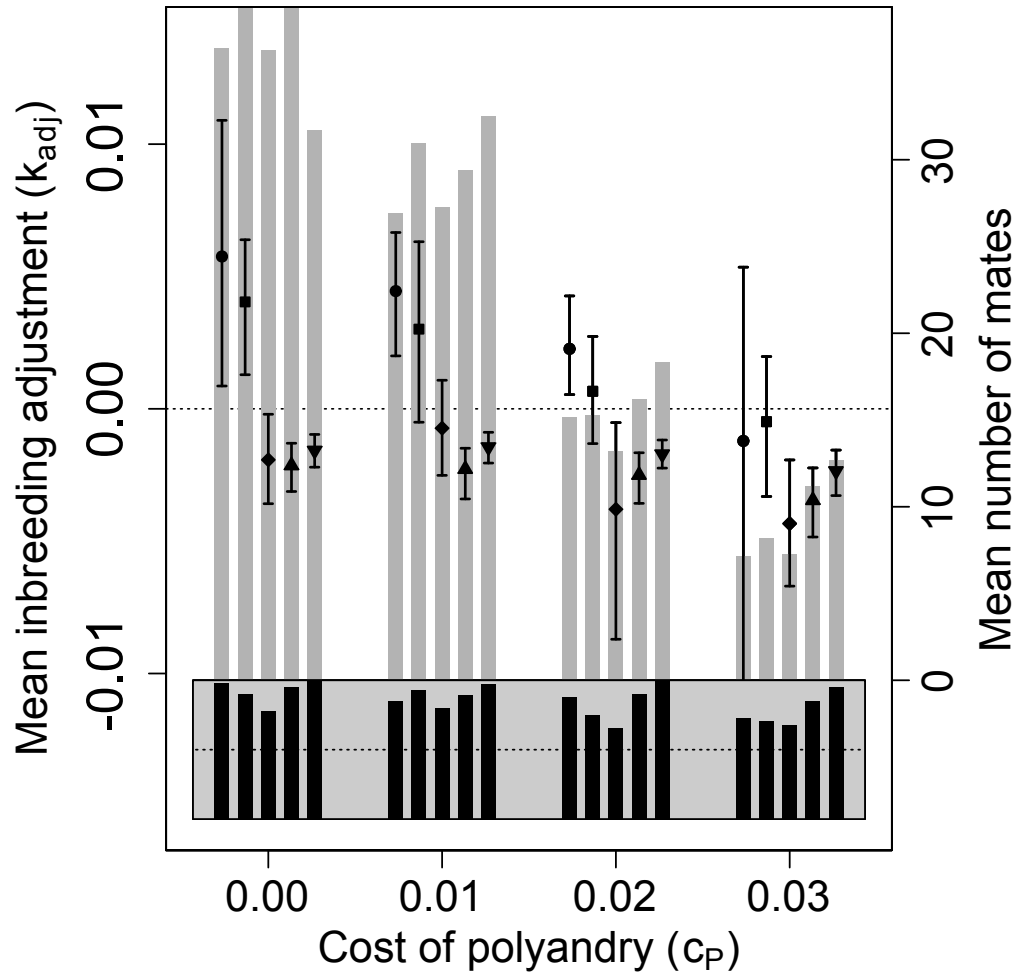




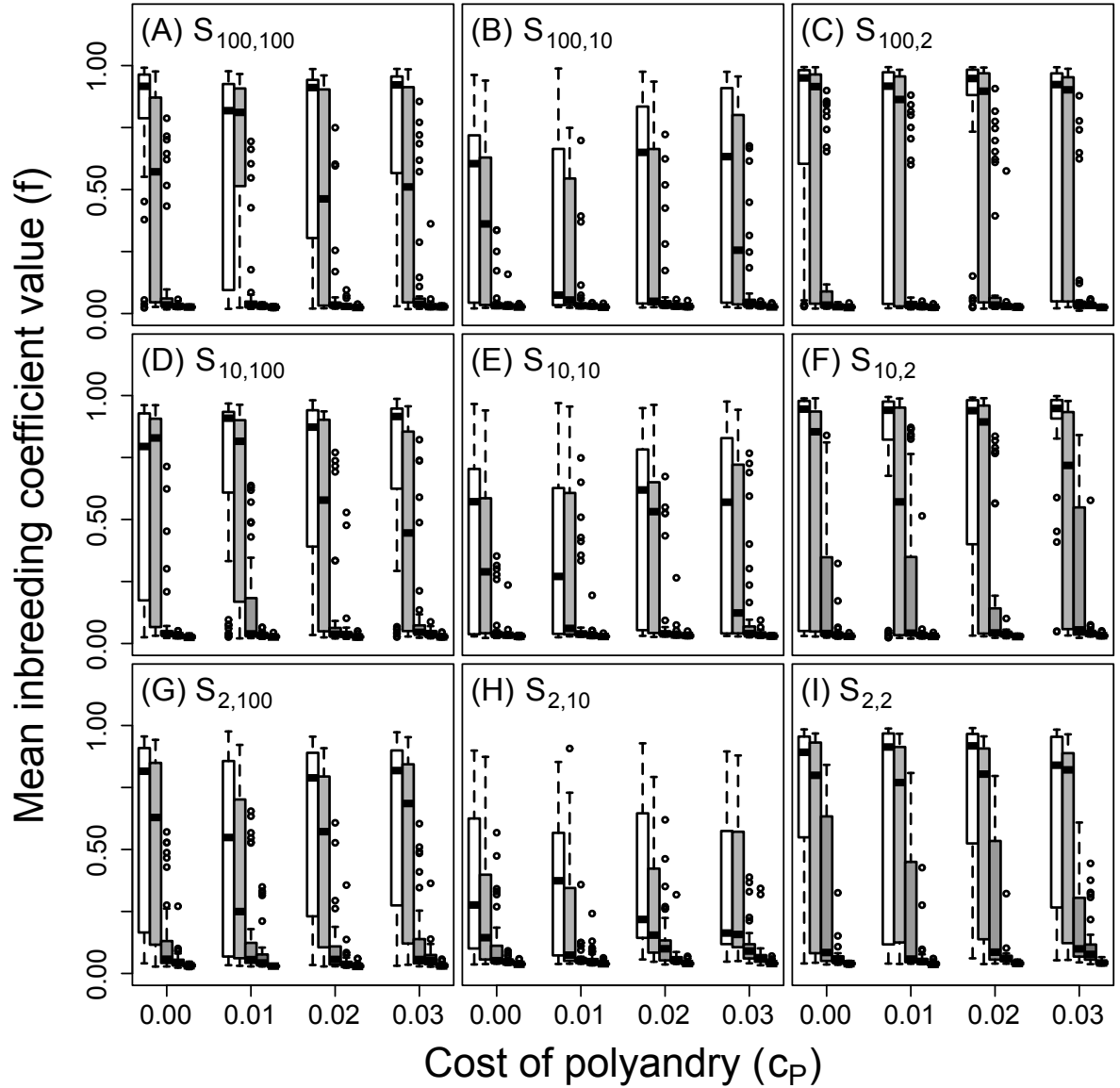
**Figure S2-7:** Distributions of mean polyandry allele (A) value ( $P_a$ ) and phenotype (B) value ( $P_p$ ) after 5000 simulated generations across replicates with different parameter combinations when polyandry is conditional. Male availability is socially constrained ( $S_{Q,100}$ ) such that females choosing their initial mates only have access to males not already chosen by other females. Blocks of boxes within A and B show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five increasingly severe magnitudes of inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. The dotted horizontal line in A indicates zero on the y-axis. Grey vertical bars highlight replicate simulations in which expected values (i.e., grand means) of mean  $P_a$  are positive and 95% bootstrapped confidence intervals do not overlap zero.



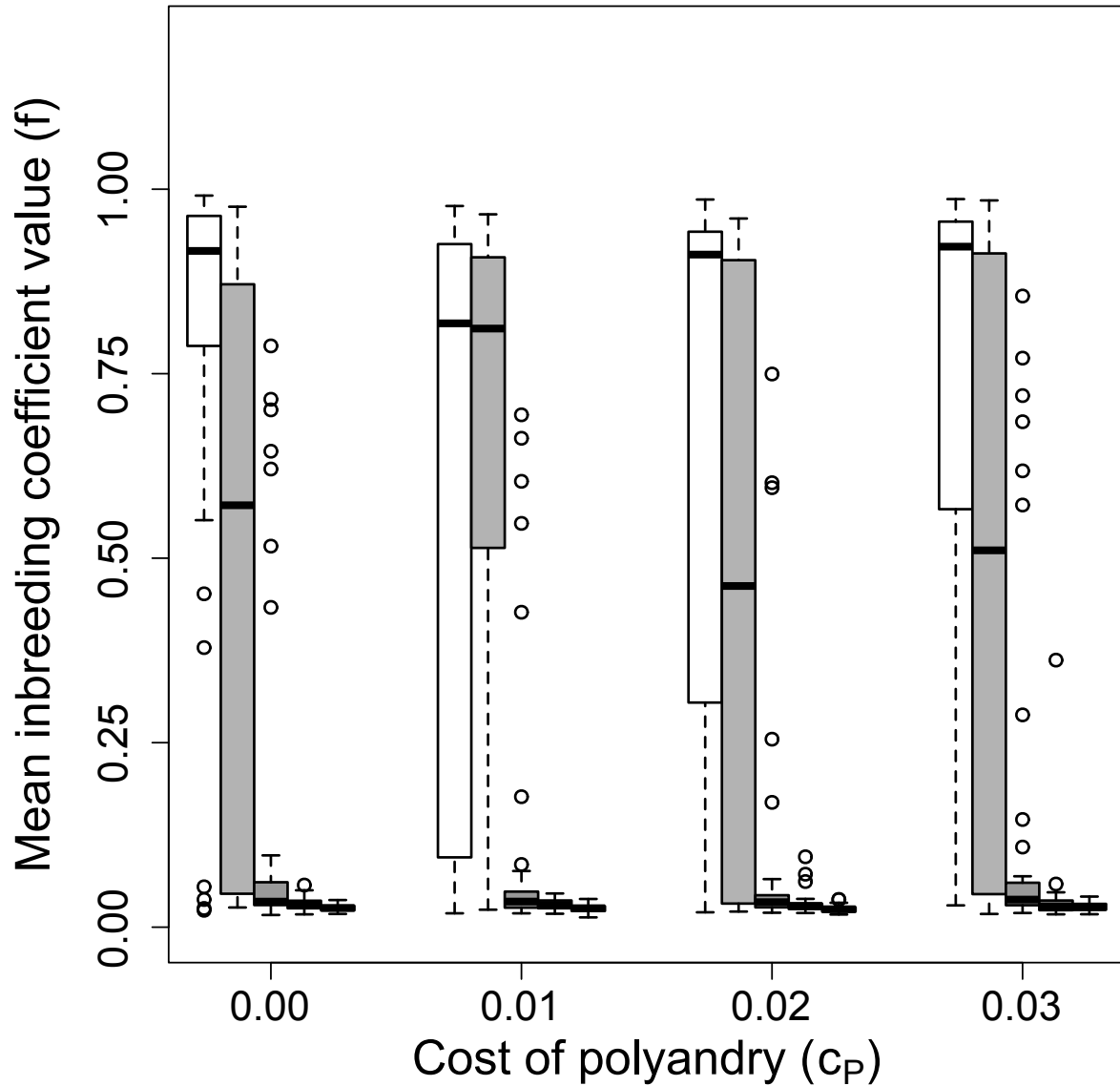
**Figure S2-8:** Mean inbreeding adjustment ( $k_{adj}$ ) through polyandry in generation 5000 across replicate simulations with different parameter combinations when polyandry is conditional. Panels show different combinations of initial versus additional male availability ( $S_{initial,additional}$ ) for choosing females. Blocks of points show four direct costs of the polyandry phenotype ( $c_P$ ), and points in each block show inbreeding depression slopes ( $\beta$ ) of 0 ( $\bullet$ ), 0.2 ( $\blacksquare$ ), 1 ( $\blacklozenge$ ), 2 ( $\blacktriangle$ ), and 5 ( $\blacktriangledown$ ). Each point shows the expected value (i.e., grand mean) of mean  $k_{adj}$  for 100 replicate simulations, and error bars show 95% bootstrapped confidence intervals around expected mean  $k_{adj}$ . Grey bars show the mean number of mates each female had across all replicates (right y-axis). Black bars show proportions (grey region spans 0 to 1; dotted lines indicate 0.5) of replicates in which at least one female is polyandrous.



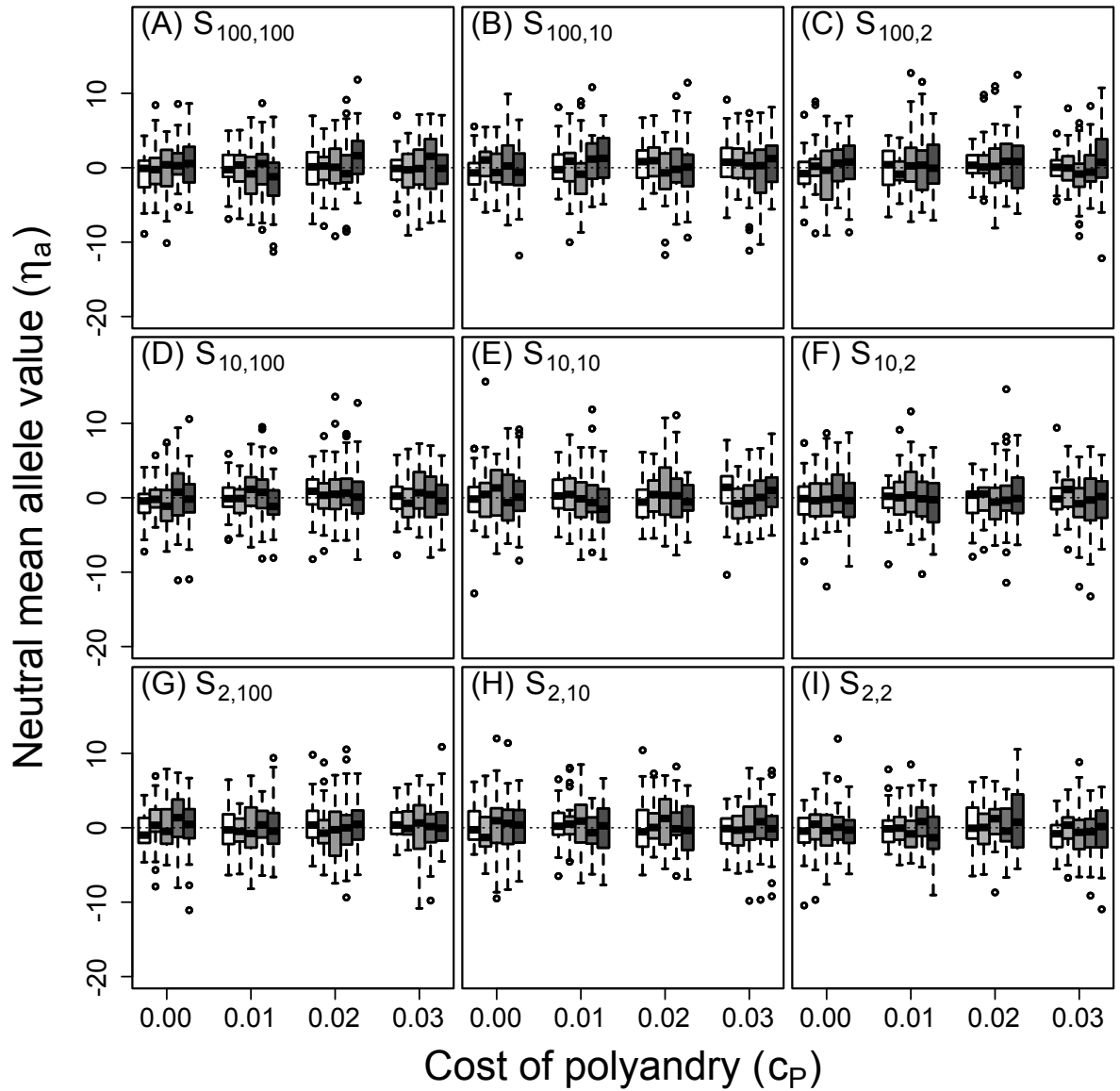
**Figure S2-9:** Mean inbreeding adjustment ( $k_{adj}$ ) through polyandry in generation 5000 across replicate simulations with different parameter combinations when polyandry is conditional. Male availability is socially constrained ( $S_{Q,100}$ ) such that females choosing their initial mates only have access to males not already chosen by other females. Blocks of points show four direct costs of the polyandry phenotype ( $c_P$ ), and points in each block show inbreeding depression slopes ( $\beta$ ) of 0 ( $\bullet$ ), 0.2 ( $\blacksquare$ ), 1 ( $\blacklozenge$ ), 2 ( $\blacktriangle$ ), and 5 ( $\blacktriangledown$ ). Each point shows the expected value (i.e., grand mean) of mean  $k_{adj}$  for 100 replicate simulations, and error bars show 95% bootstrapped confidence intervals around expected mean  $k_{adj}$ . Grey bars show the mean number of mates each female had across all replicates (right y-axis). Black bars show proportions (grey region spans 0 to 1; dotted lines indicate 0.5) of replicates in which at least one female is polyandrous.



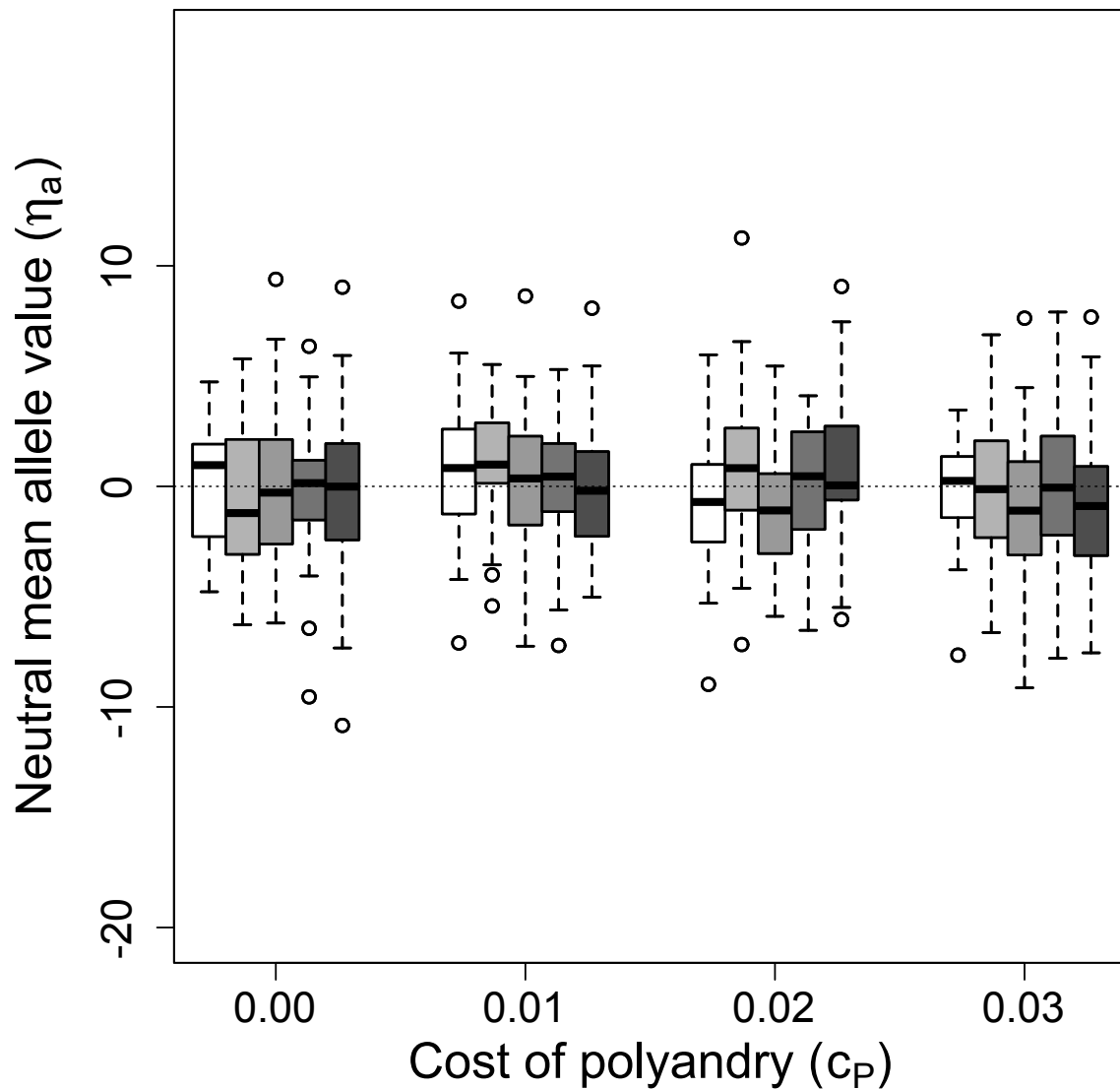
**Figure S2-10:** Distributions of mean inbreeding coefficient values ( $f$ ) after 5000 simulated generations across replicates with different parameter combinations. Panels show different combinations of initial versus additional male availability ( $S_{initial,additional}$ ) for choosing females. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Overall, mean  $f$  varied greatly among replicates when  $\beta < 1$ , ranging from 0–1. High  $f$  in these replicates was caused by evolution of inbreeding preference. When  $\beta \geq 1$ , mean  $f$  was nearly always low, as caused by evolution of inbreeding avoidance.



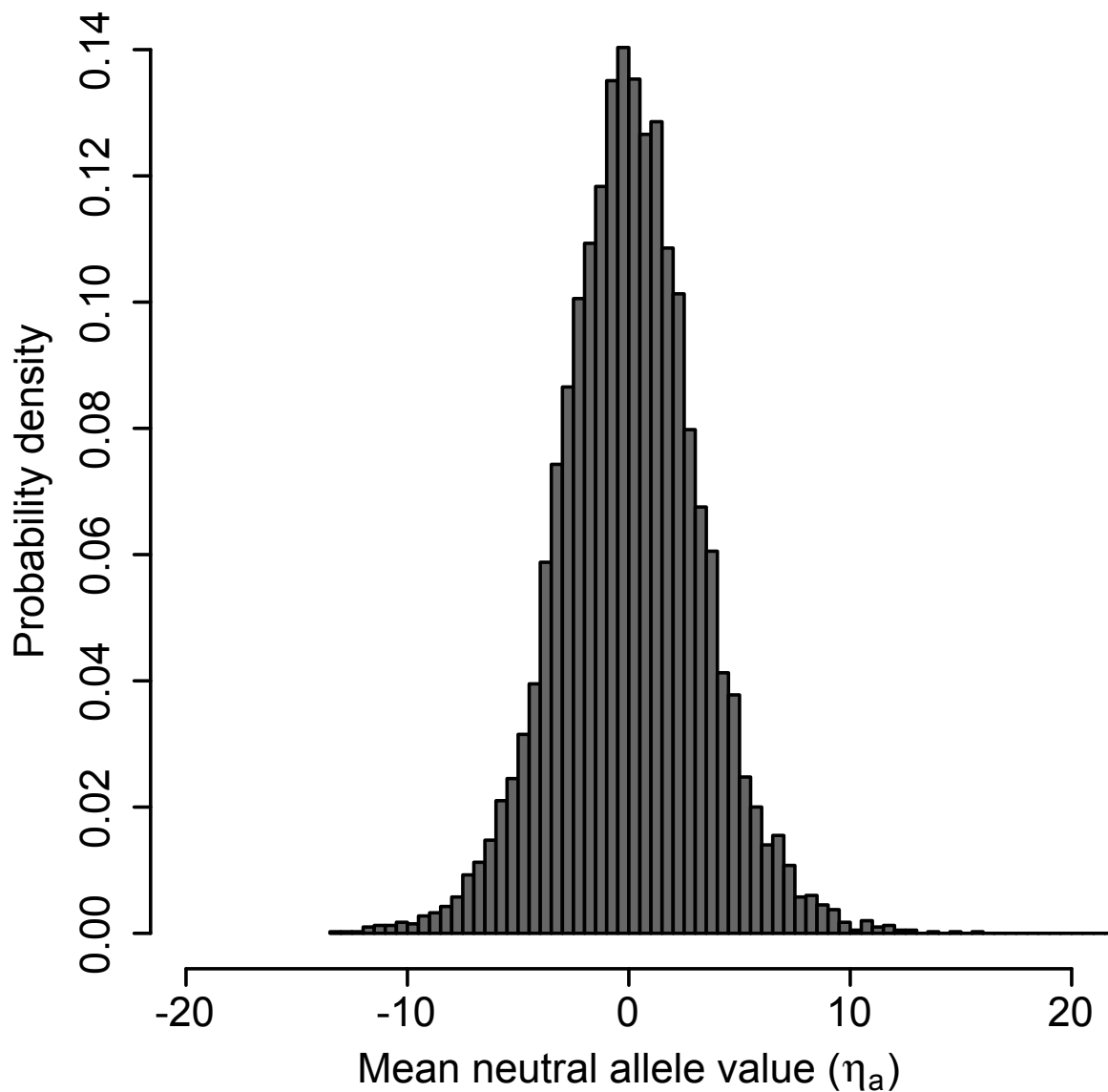
**Figure S2-11:** Distributions of mean inbreeding coefficient values ( $f$ ) values after 5000 simulated generations across replicates with different parameter combinations. Male availability is socially constrained ( $S_{Q,100}$ ) such that females choosing their initial mates only have access to males not already chosen by other females. Blocks of boxes show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Overall, mean  $f$  varied greatly among replicates when  $\beta < 1$ , ranging from 0 – 1. High  $f$  in these replicates was caused by evolution of inbreeding preference. When  $\beta \geq 1$ , mean  $f$  was nearly always low, as caused by evolution of inbreeding avoidance.



**Figure S2-12:** Distributions of mean allele values with neutral effects ( $\eta_a$ ) after 5000 simulated generations across replicates with different parameter combinations. Panels show different combinations of initial versus additional male availability ( $S_{initial,additional}$ ) for choosing females. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis.

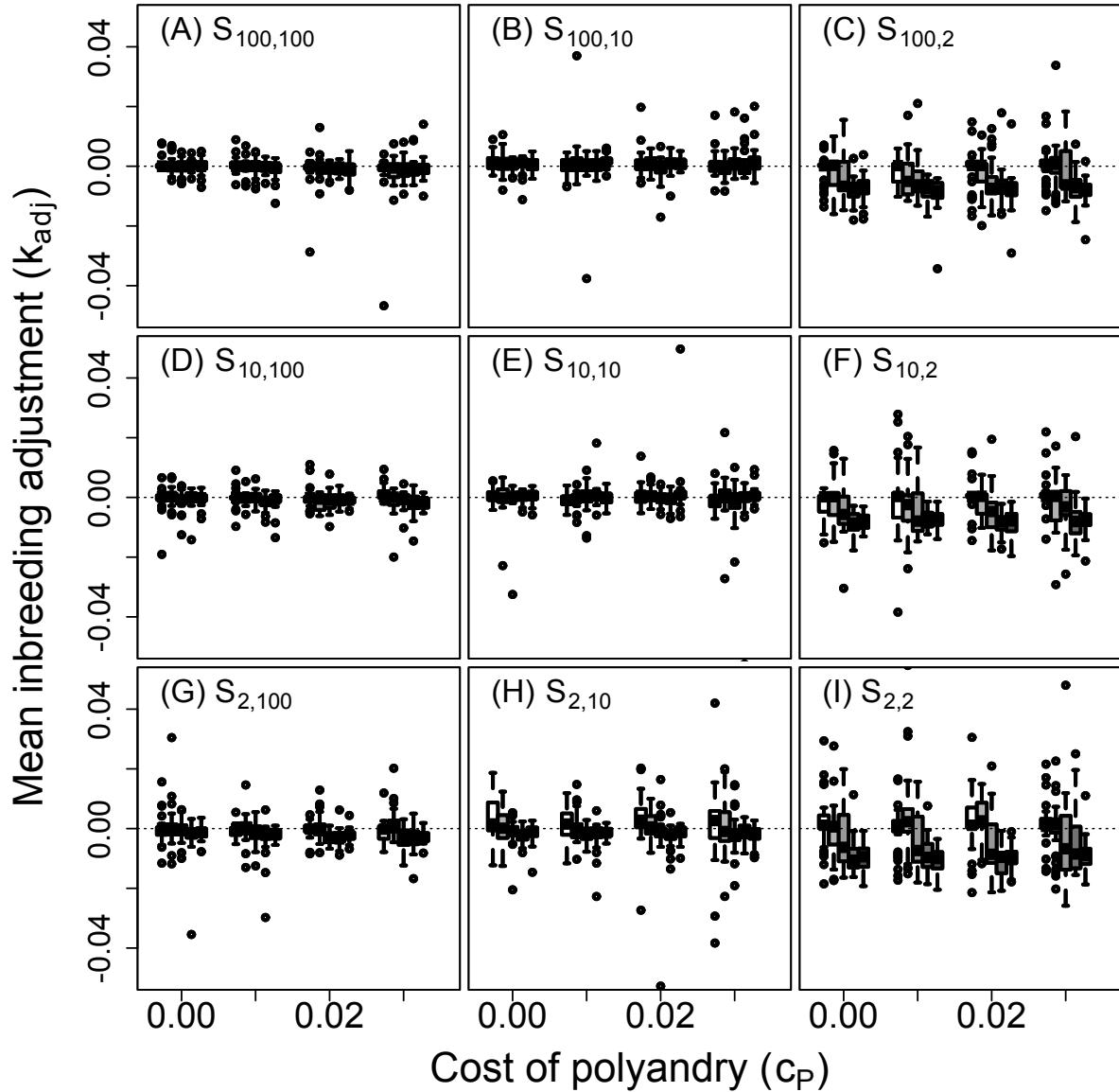


**Figure S2-13:** Distributions of mean values of alleles with neutral effect ( $\eta_a$ ) after 5000 simulated generations across replicates with different parameter combinations. Male availability is socially constrained ( $S_{Q,100}$ ) such that females choosing their initial mates only have access to males not already chosen by other females. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis.

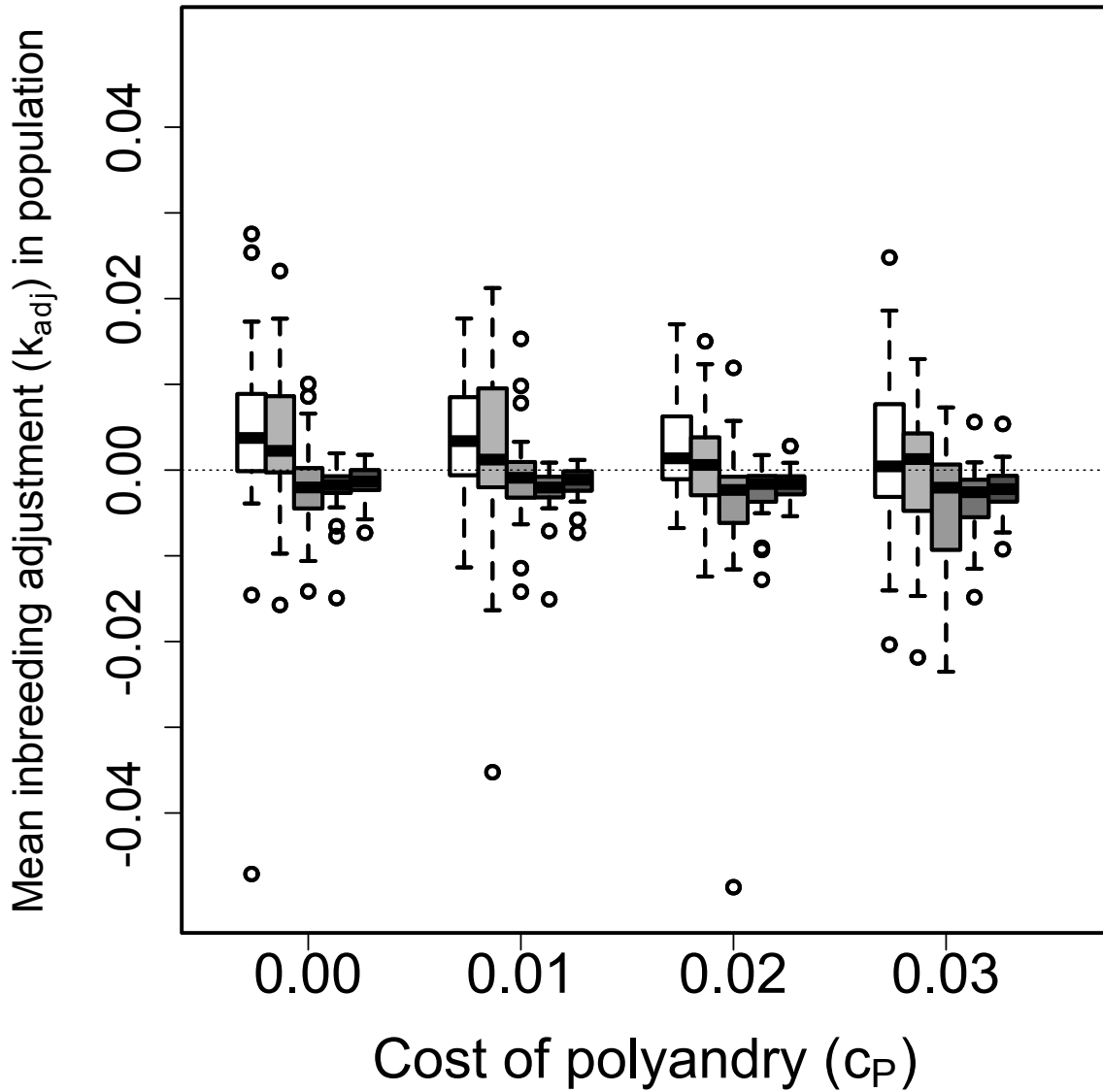


**Figure S2-14:** Distributions of mean values of alleles with neutral effect ( $\eta_a$ ) among all simulations. Frequencies of  $\eta_a$  after 5000 generations were unaffected by parameter values (see Figure S2-9 on p. S2-11), so here they are pooled to show the estimated mean (-0.034) and standard deviation (3.27) of  $\eta_a$  allele values across all parameter combinations. Allele values did not differ significantly from zero, as expected a priori. Therefore, because neutral allele frequencies are unaffected by selection and expected to be zero after 5000 generations, values of alleles underlying inbreeding strategy  $I_a$  and polyandry  $P_a$  can be compared against this neutral expectation to infer selection.

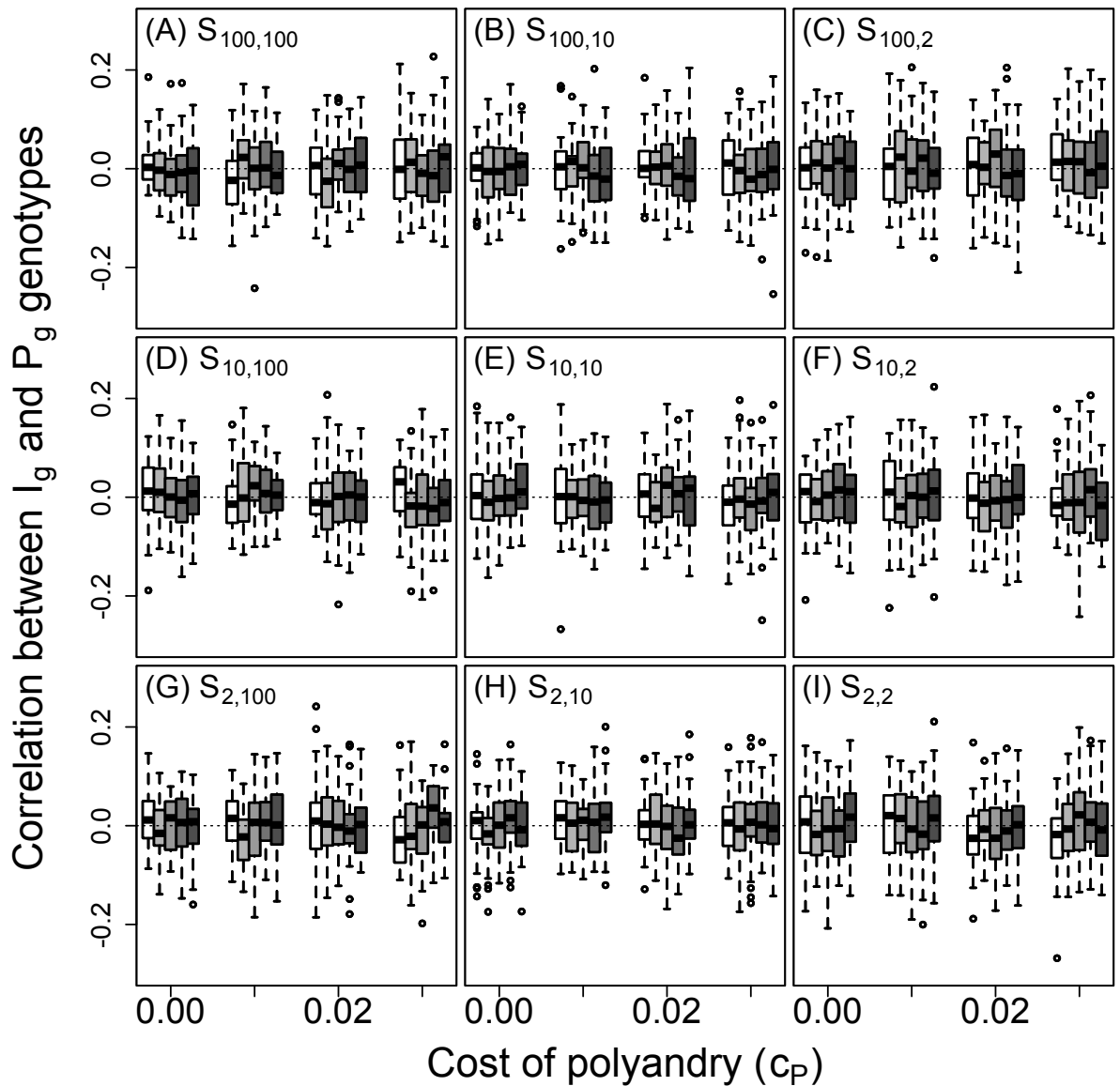




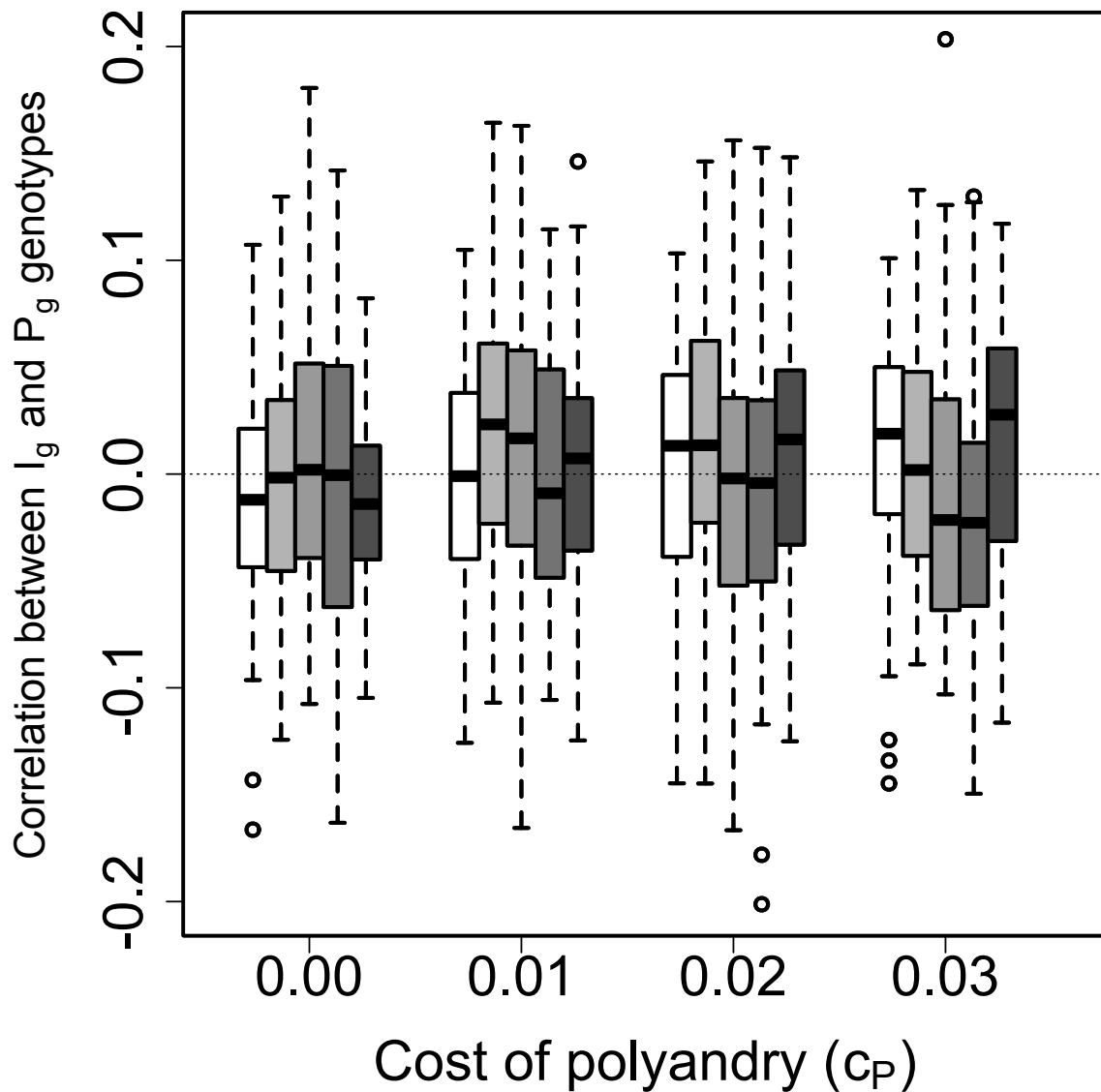
**Figure S2-15:** Distributions of mean inbreeding adjustment ( $k_{adj}$ ) through polyandry in generation 5000 across replicate simulations with different parameter combinations. Panels show different combinations of initial versus additional male availability ( $S_{initial,additional}$ ) for choosing females. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five increasingly severe magnitudes of inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (left to right). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis. Across most simulations the magnitude of  $k_{adj}$  does not exceed 0.01, and magnitudes  $> 0.02$  are very rare, suggesting that mean kinship adjustment is unlikely to be large given conditional dependent polyandry.



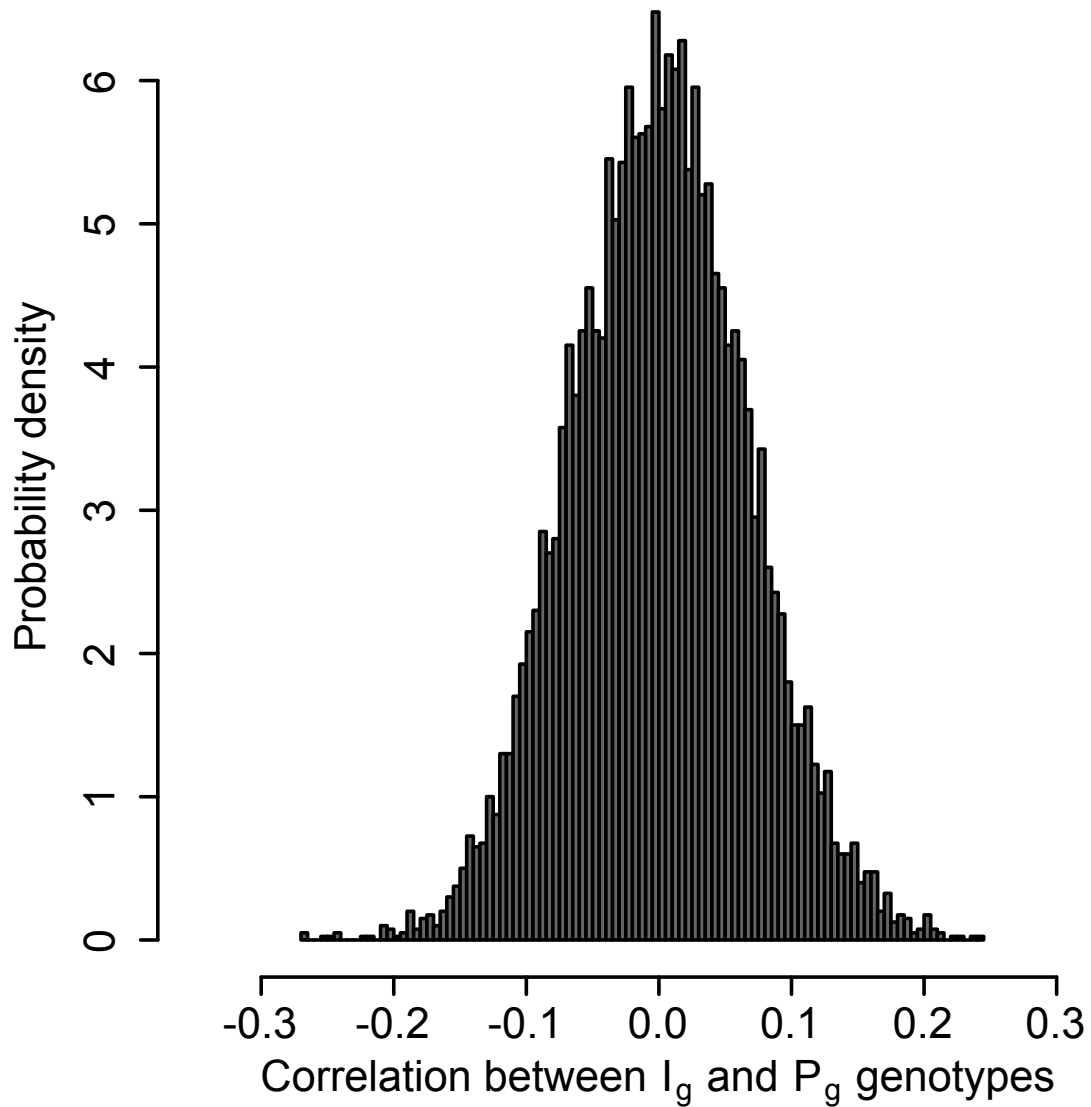
**Figure S2-16:** Distributions of mean inbreeding adjustment ( $k_{adj}$ ) through polyandry in generation 5000 across replicate simulations when male availability is socially constrained ( $S_{Q,100}$ ) such that females choosing their initial mates only have access to males not already chosen by other females. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis. As in other  $S_{initial,additional}$  combinations, magnitudes of  $k_{adj}$  were rare, therefore suggesting that mean kinship adjustment is unlikely to be large given social mating constraints and conditional polyandry.



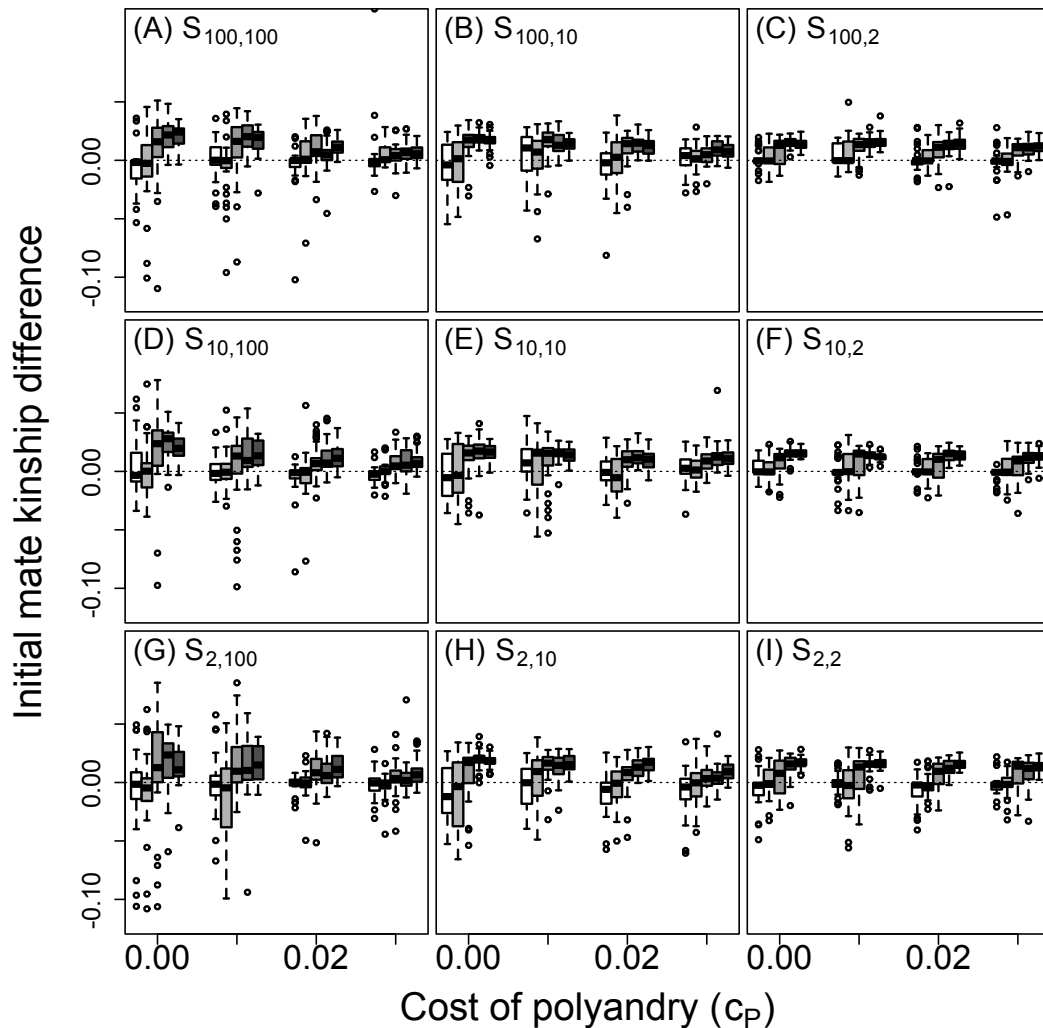
**Figure S2-17:** Distributions of the correlation between inbreeding strategy ( $I_g$ ) and polyandry ( $P_g$ ) genotypes among individuals within simulated populations in generation 5000. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis. Distributions do not show any clear tendency for correlations between  $I_g$  and  $P_g$ , and therefore no evidence of evolutionary feedbacks or runaway selection between inbreeding strategy and polyandry traits when polyandry is conditional.



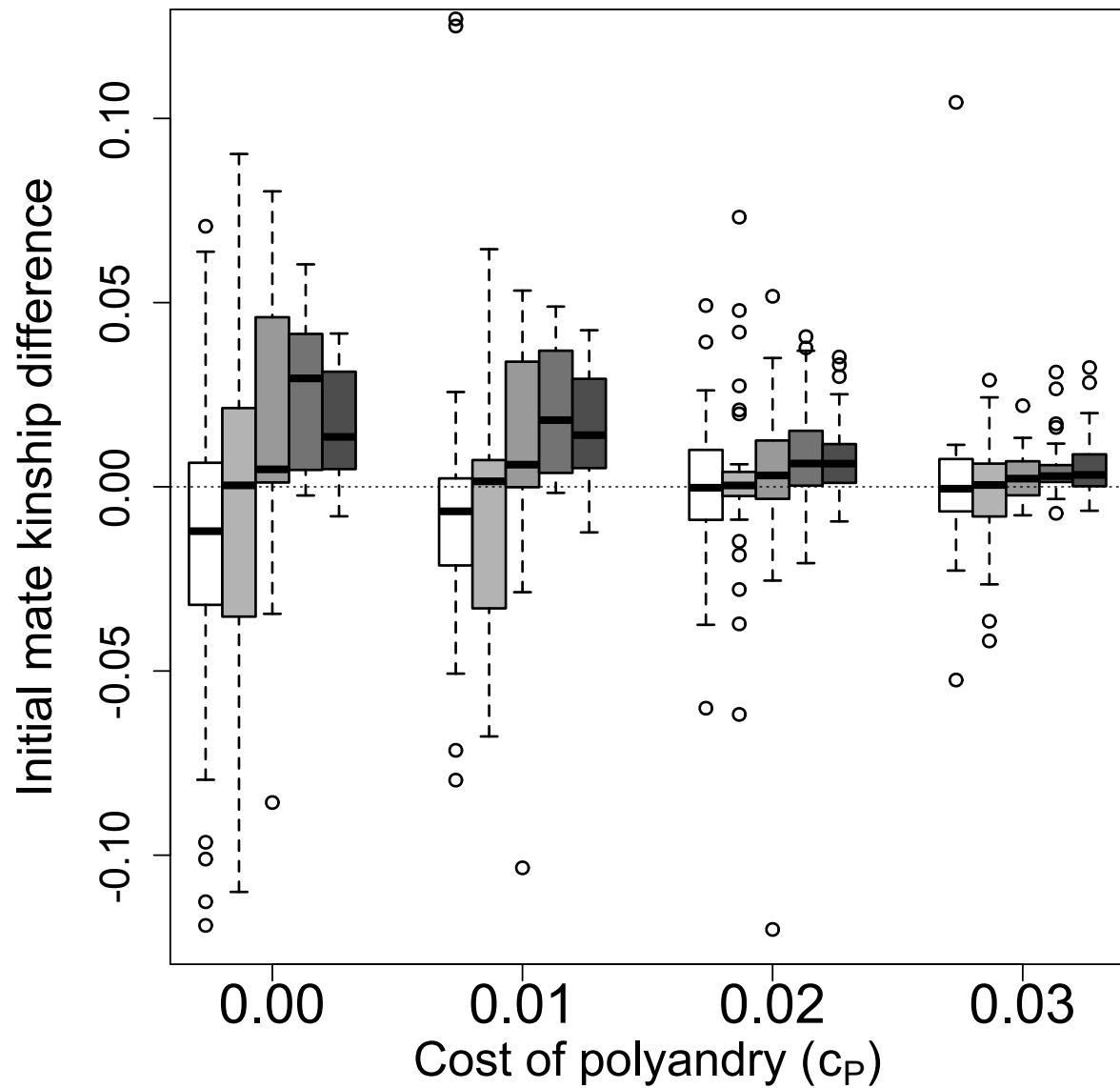
**Figure S2-18:** Distributions of the correlation between inbreeding strategy ( $I_g$ ) and polyandry ( $P_g$ ) genotypes among individuals within simulated populations in generation 5000 when male availability is socially constrained ( $S_{Q,100}$ ) such that females choosing their initial mates only have access to males not already chosen by other females, and when polyandry is conditional. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis. As in simulations where male availability is not socially constrained (p. S2-14), there is no clear trend in these distributions and therefore no evidence for evolutionary feedbacks between inbreeding strategy and polyandry.



**Figure S2-19:** Distributions of the correlation between inbreeding strategy ( $I_g$ ) and polyandry ( $P_g$ ) genotypes among individuals within simulated populations in generation 5000 among all simulations. The normal distribution centred on a mean near zero further highlights the lack of correlation between inbreeding strategy and polyandry genotypes when polyandry is conditional.



**Figure S2-20:** Distributions of the mean kinship between polyandrous females and their initial mate choices minus the mean kinship between monandrous females and their initial mate choices within simulated populations in generation 5000 (i.e., the extent to which females that engage in polyandry are more related to their initial mates than their monogamous counterparts within the same population). Positive values reflect populations in which polyandrous females are more closely related to their initial mate than monandrous females. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis. Due to strict conditional dependence, females are consistently more likely to engage in polyandry if their initial mate choice is closely related and  $\beta$  is high. But the mean difference in kinship between a polyandrous female and her initial mate and a monandrous female and her initial mate rarely exceeded 0.05, and was typically ca 0.025, suggesting that such differences might be difficult to detect in wild populations.



**Figure S2-21:** Distributions of the mean kinship between polyandrous females and their initial mate choices minus the mean kinship between monandrous females and their initial mate choices within simulated populations in generation 5000 (i.e., the extent to which females that engage in polyandry are more related to their initial mates than their monogamous counterparts within the same population) when male availability is socially constrained ( $S_{Q,100}$ ) such that females choosing their initial mates only have access to males not already chosen by other females, and when polyandry is conditional. Blocks of boxes within panels show four direct costs of the polyandry phenotype ( $c_P$ ). Boxes within blocks show five magnitudes of increasingly severe inbreeding depression  $\beta = \{0, 0.2, 1.0, 2.0, 5.0\}$  (white to dark grey). Central lines on boxes show medians across 100 replicate simulations, box limits show inter-quartile ranges, whiskers show  $1.5 \times IQRs$ , and extreme points show outliers. Dotted horizontal lines indicate zero on the y-axis.